

1. Compute the following integrals. The contour of integration can be any curve that joins the two points.

$$(a) \int_i^{i/2} e^{\pi z} dz, \quad (b) \int_0^{\pi+2i} \cos \frac{z}{2} dz, \quad (c) \int_1^3 (z-2)^3 dz.$$

2. Let C be a simple closed curve that does not go through the point z_0 . If $n \in \mathbb{Z} \setminus \{0\}$ show that

$$\oint_C (z - z_0)^{n-1} dz = 0.$$

What happens if $n = 0$?

3. Let C be the circle with center at 0 and radius 1/2, positively oriented. Compute

$$\oint_C \frac{dz}{z(z-1)}.$$

Hint: $\frac{1}{z(z-1)} = \frac{1}{z-1} - \frac{1}{z}.$